

Coulomb Effects in High Intensity Drivers

Workshop on the Future of High Energy Physics

Snowmass, July 5, 2001

I. Hofmann

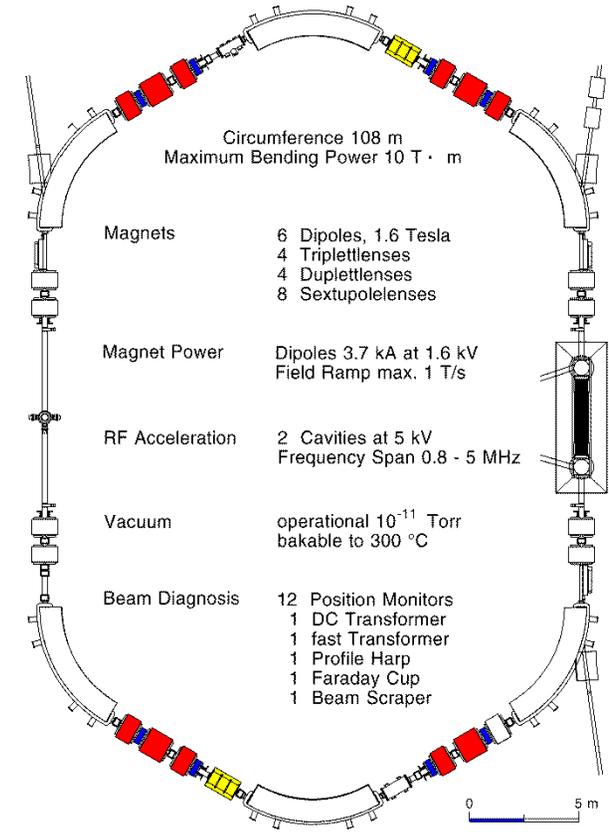
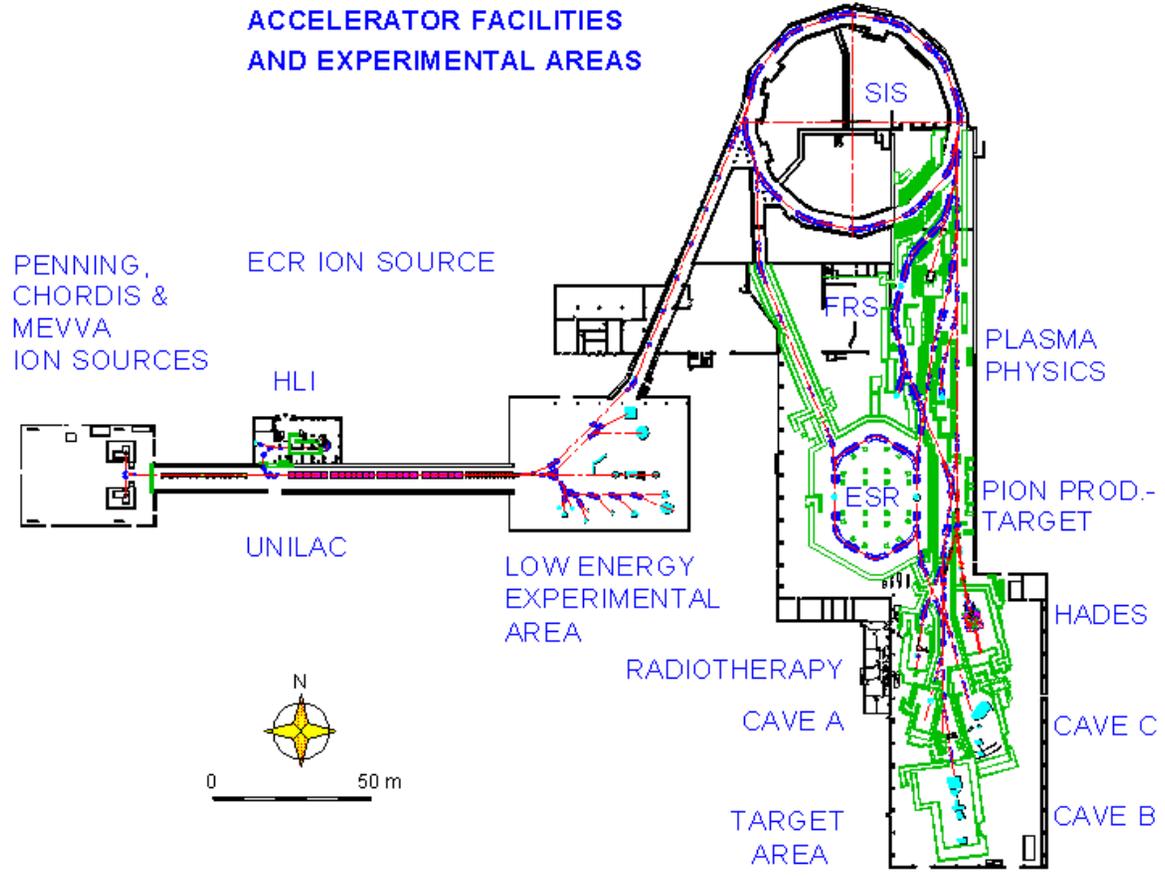
GSI Darmstadt

Outline

- Space Charge & Longitudinal Phase Space
 - Stabilizing effects
 - Measurement issues
 - Compression
- Transverse Space Charge Effects
 - Quadrupolar measurements
 - Space charge resonance
 - Mismatch & Loss

co-workers: R. Bär, O. Boine-Frankenheim, G. Franchetti, G. Rumolo

Experimental Storage Ring for heavy ions at GSI



“History” of Longitudinal Instability

Longitudinal (resistive or microwave) instability of coasting beams or long bunches

Linear theory in 60's:

L.J. Laslett, V.K. Neil and A.M. Sessler, 1961

A.G. Ruggiero and V.C. Vaccaro, 1968 etc.

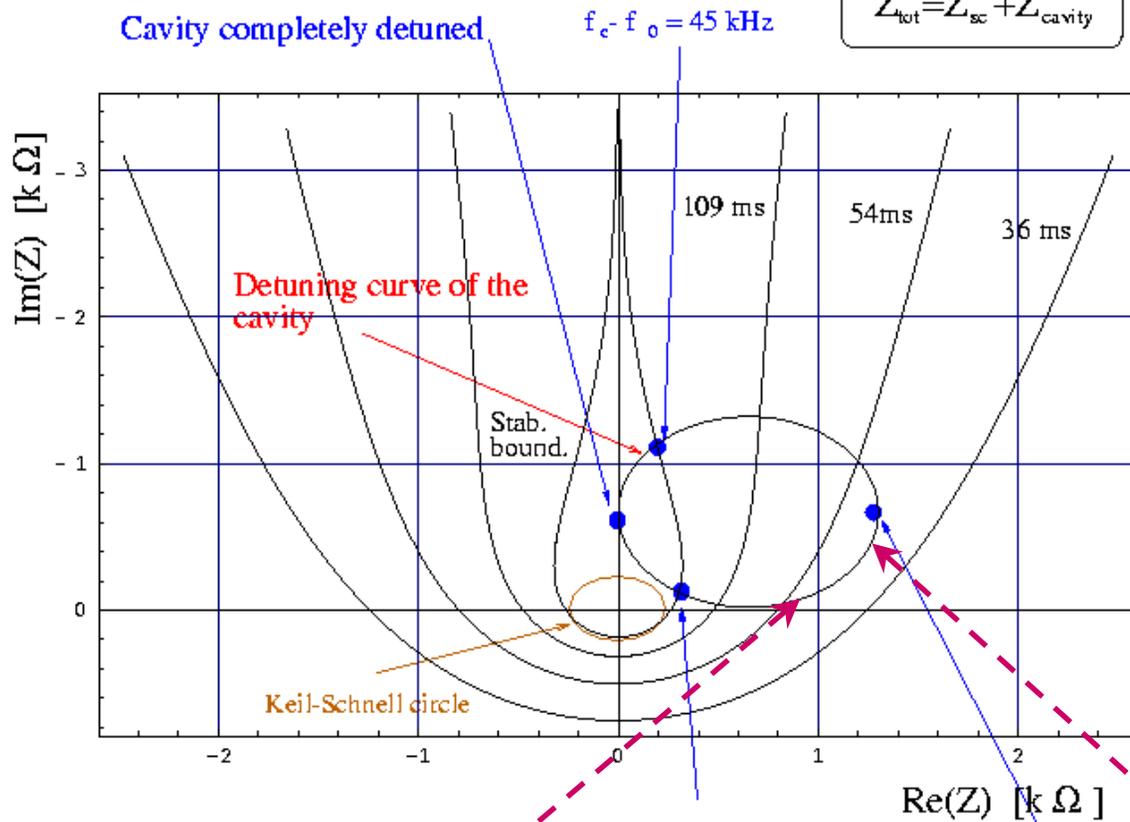
Keil-Schnell circle criterion

In Heavy Ion Fusion drivers, recently also proton drivers interest appeared to operate outside Keil-Schnell circle in space-charge-dominated regime

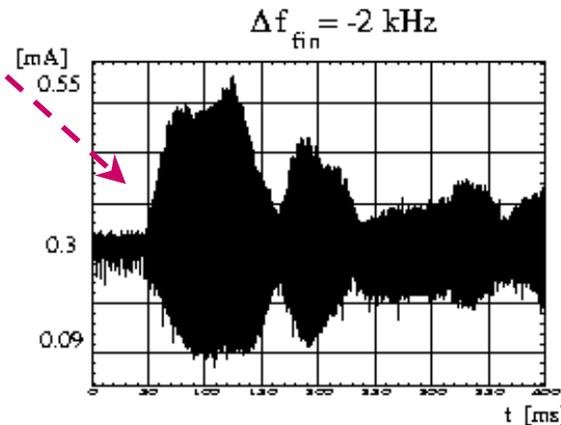
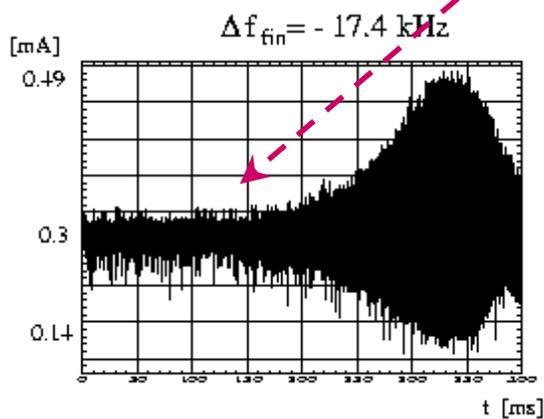
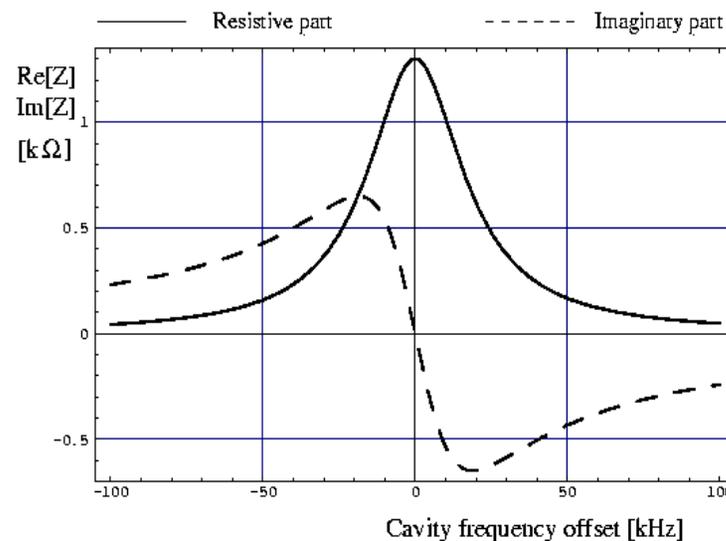
Microwave instability measured below transition (CERN-PS) ~ 30 GeV

RF cavity detuning effect on working point

$$Z_{\text{tot}} = Z_{\text{sc}} + Z_{\text{cavity}}$$



RF cavity impedance (ferrite)

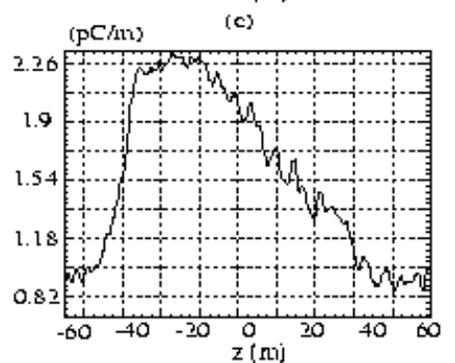
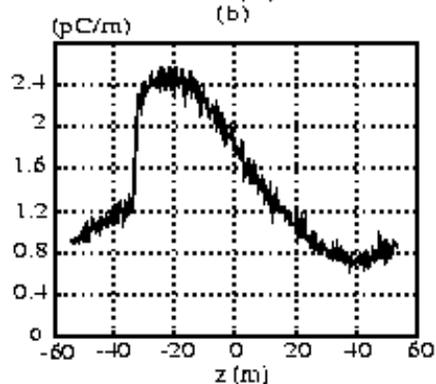
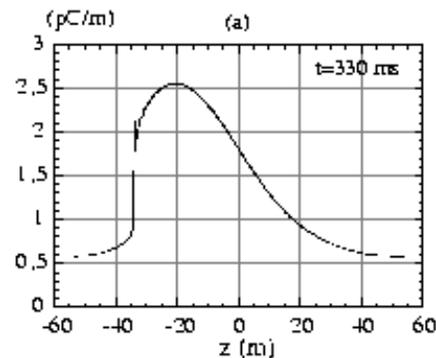


Steepening of resistively driven waves a nonlinear effect

Fluid model (warm)
- no real saturation
(goes on)

PIC

Measurement

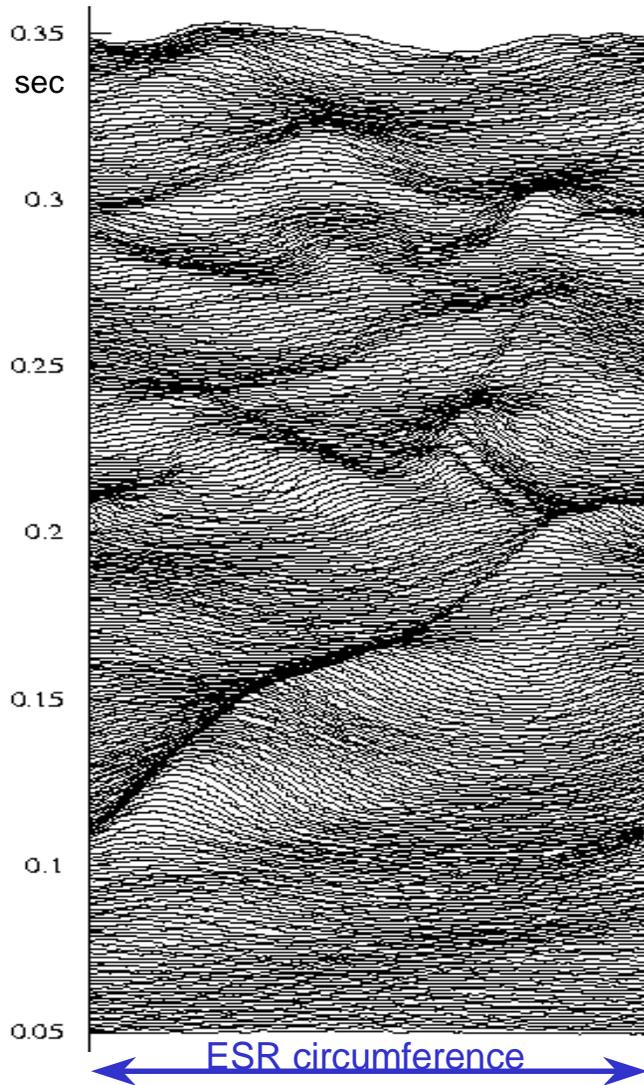


←→
ESR circumference

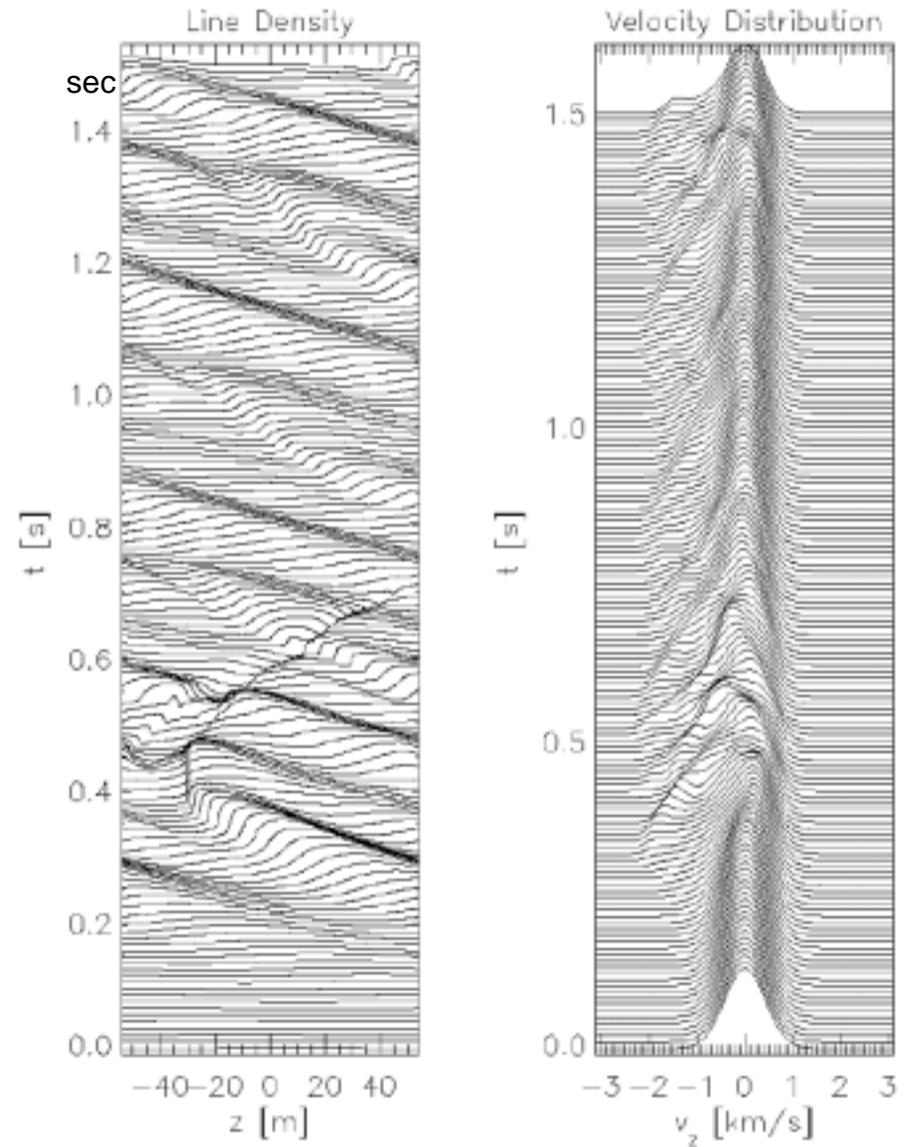
Comparison: Rumolo et al., Phys. Plasmas **6**, 1999

Mountain range diagrams have shown absence of real saturation (Landau damping) - memory effect

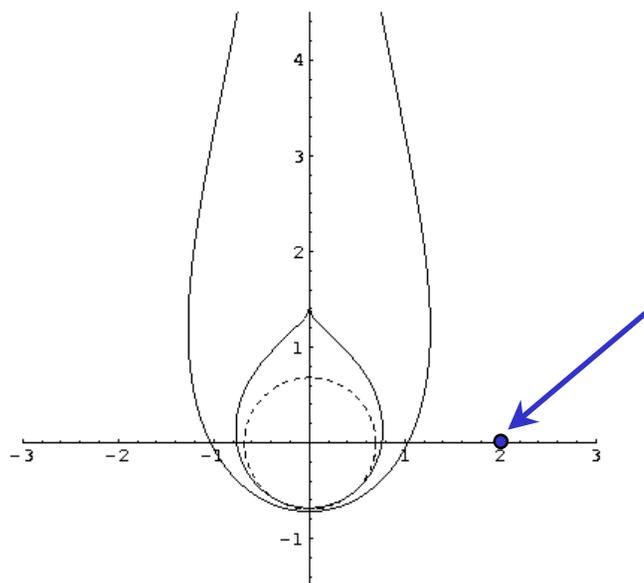
Experiment



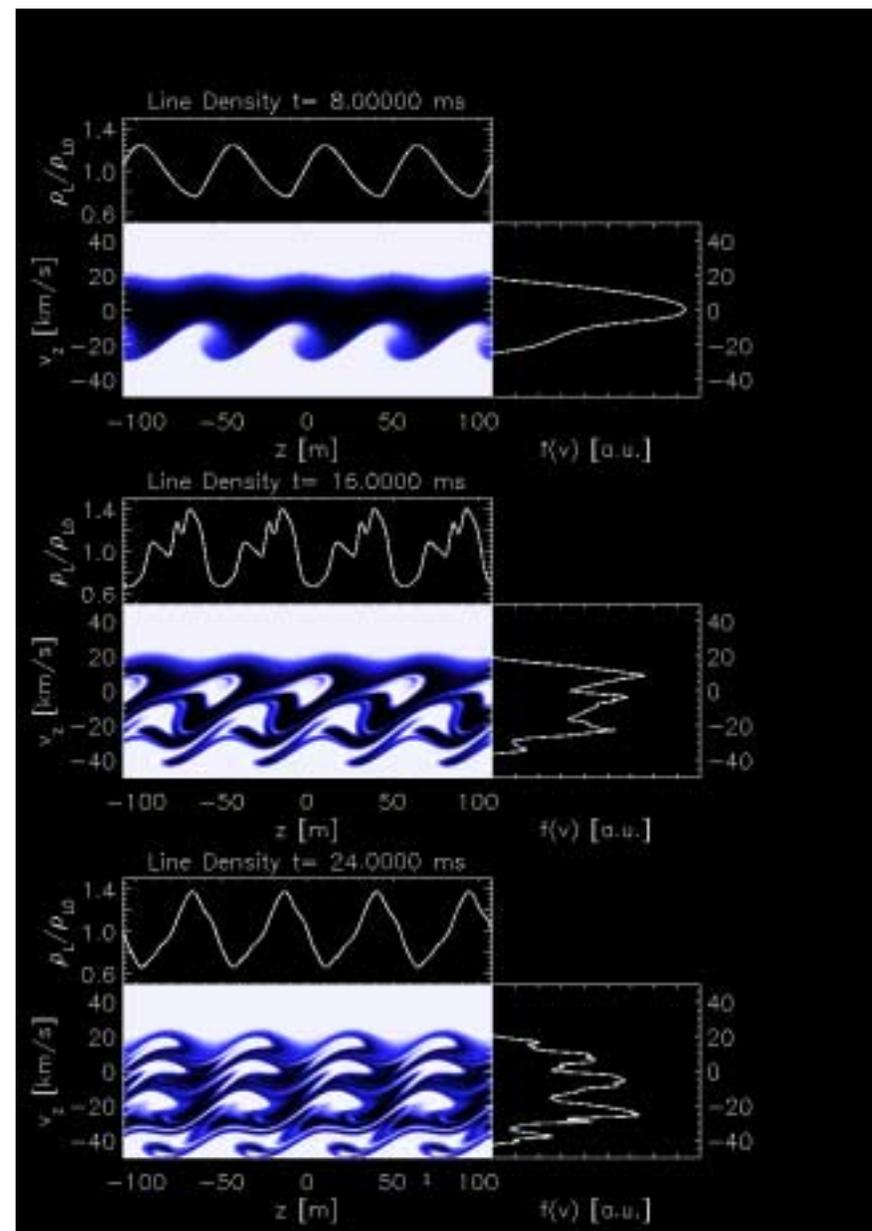
(Direct) Vlasov Simulation



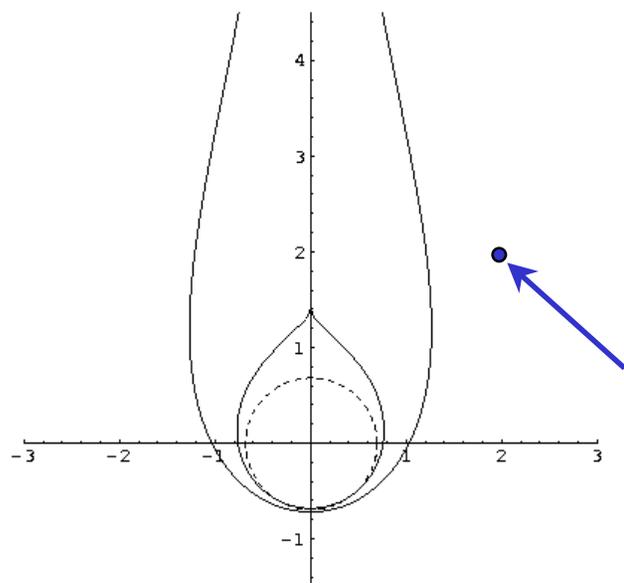
Purely resistive impedance: broadening effect



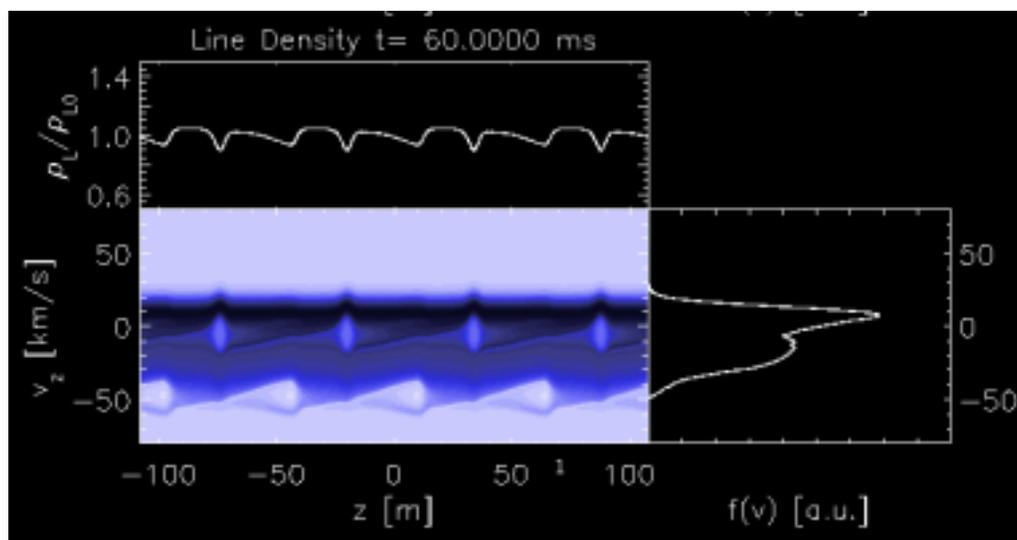
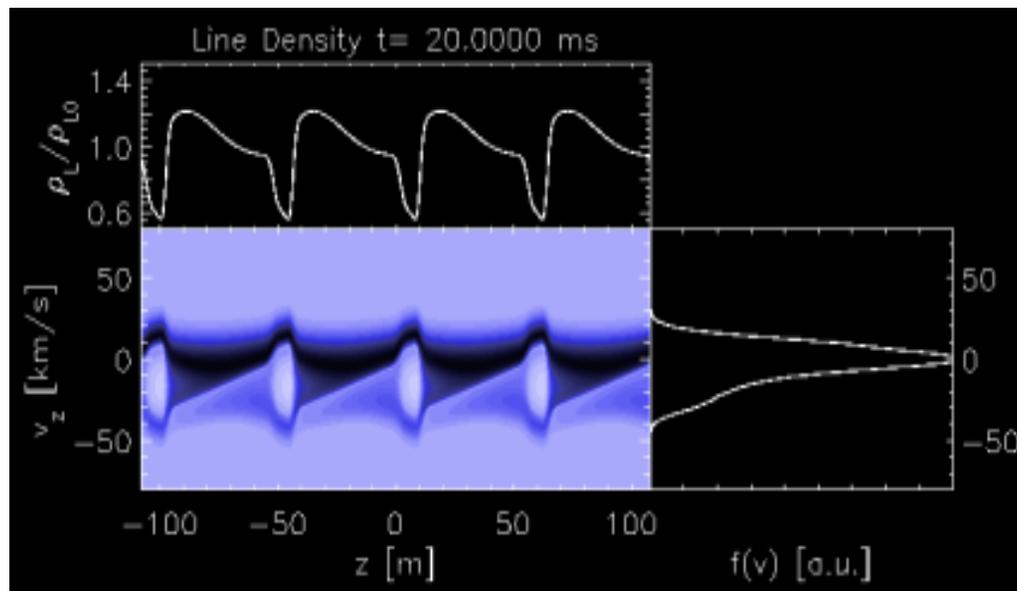
- typical behavior at higher energy
- layers of self-trapped buckets generated at lower edge of momentum space (slow wave) with strong progressive filamentation
- results in broadening (to lower momenta)



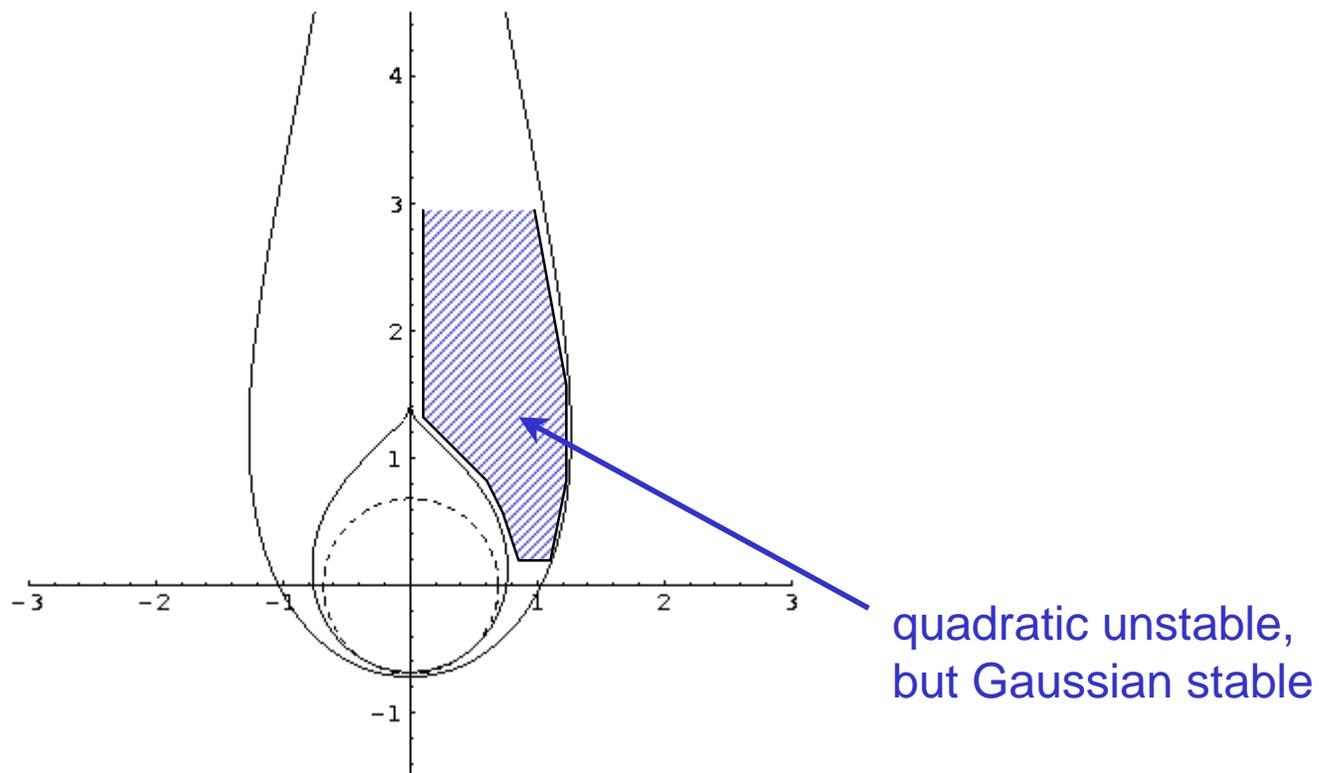
Balanced impedance (ReZ~ImZ)



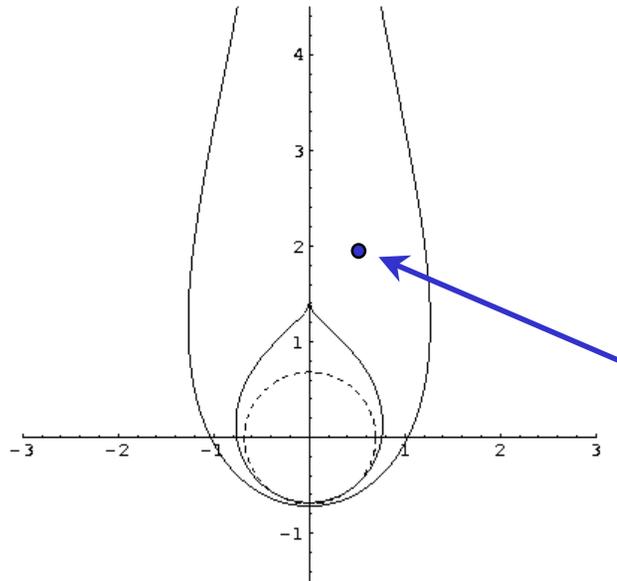
similar to ESR experiment: layers of holes traveling through momentum space and causing broadening of momentum distribution



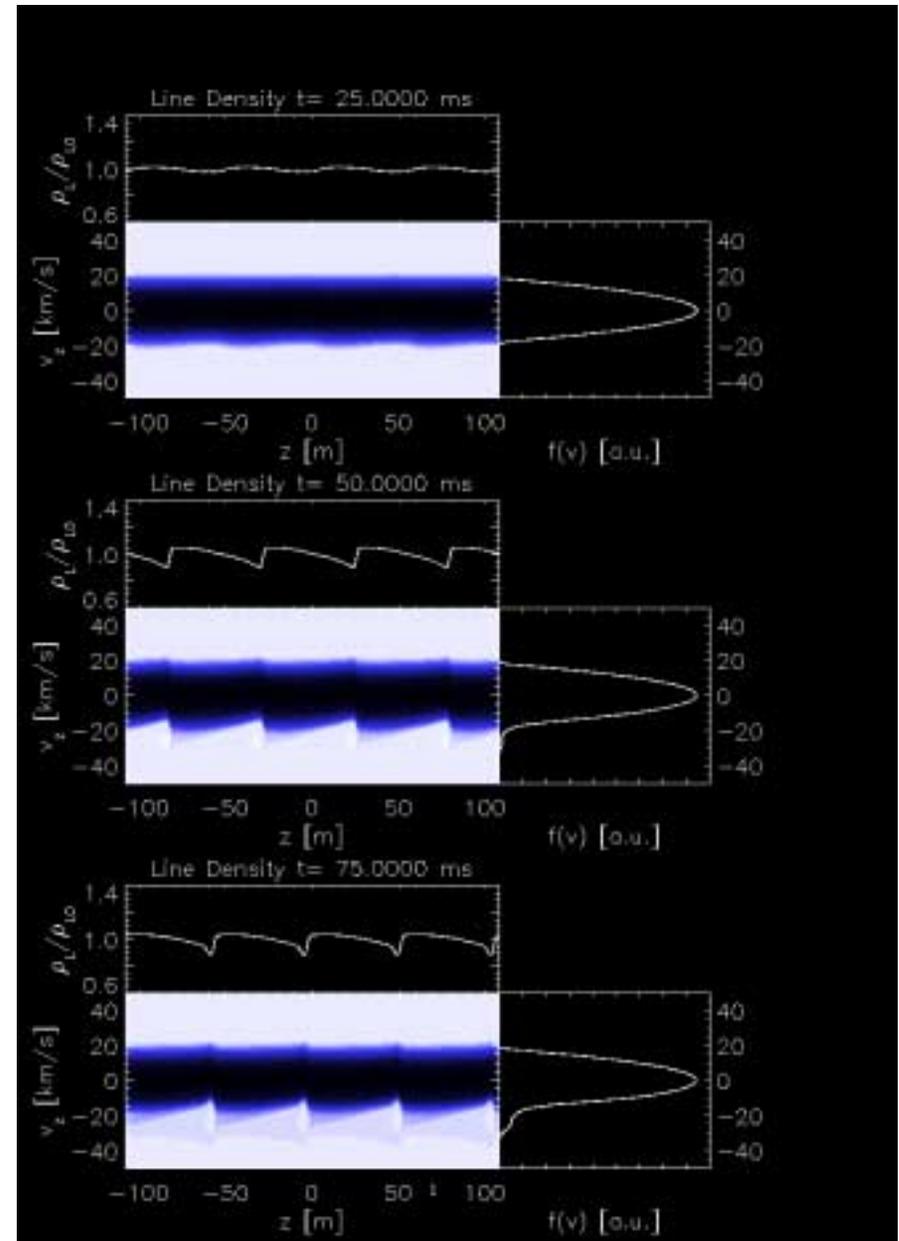
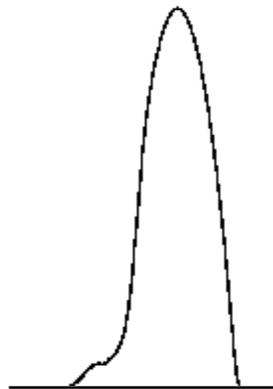
Near stability boundary



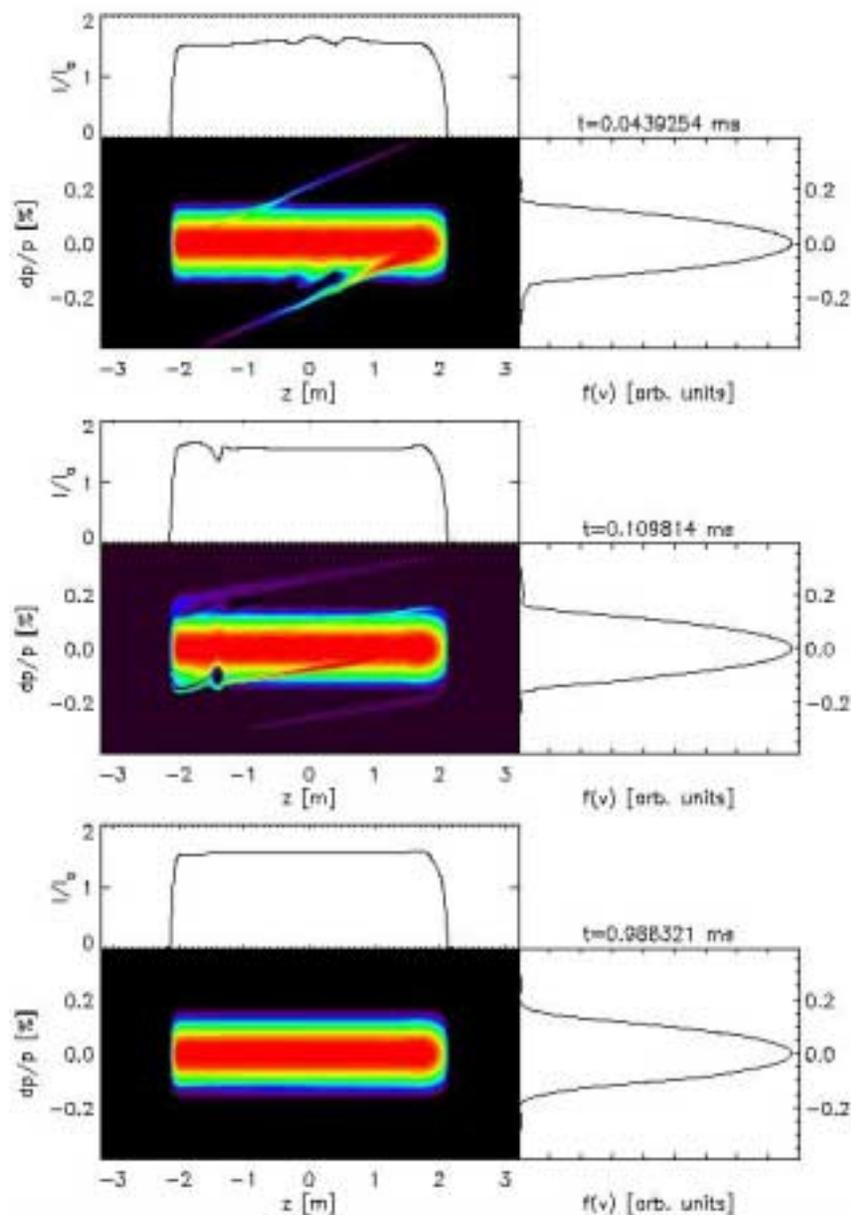
Simulation of marginally unstable distributions



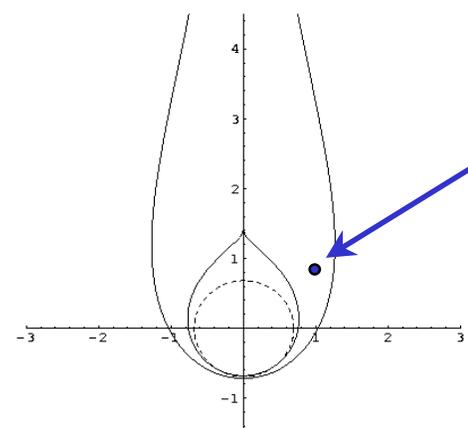
- initially parabolic (unstable)
- stabilizing tail developing here



Bunch in ideal barrier bucket with reference to a proton driver

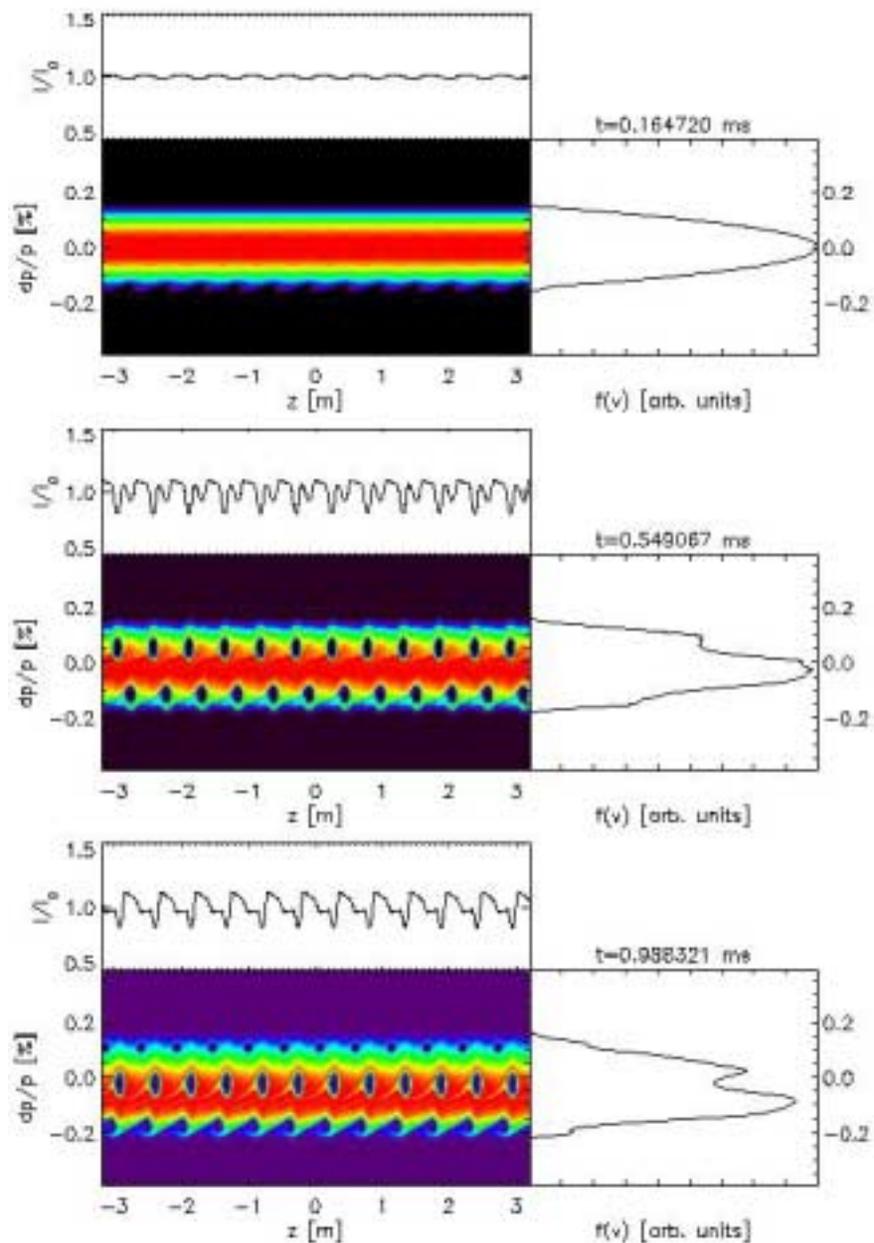


$N_{\text{bunch}}=10^{12}$ 2.2 GeV 12 ns
 Initially parabolic momentum distribution
 Square pulse into ideal barrier
 $Z/n=70$ Ohm space charge
 $Z/n=50$ Ohm broad band

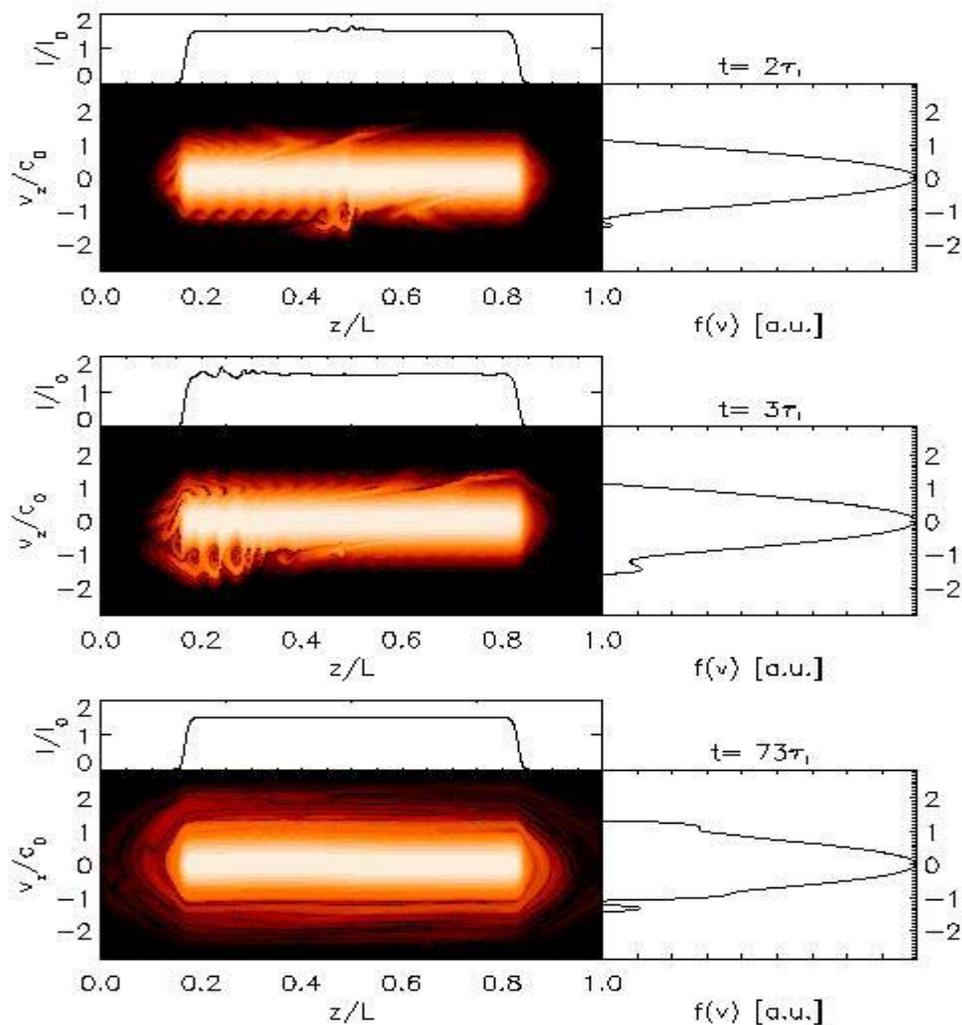


- Perturbations originating at bunch ends
- Finite bunch length can have stabilizing effect for **propagating** unstable waves
- holes trapped in phase space

Locally equivalent coasting beam shows more effect



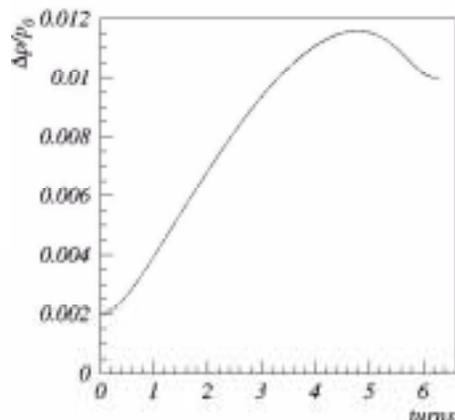
Even much more space charge dominated bunches remain stable ($U=10$, $V=1$, $h=24$)



Compression of bunches in p driver *

(ignoring higher order effects)

Example: 10^{13} p per bunch, 1.5 GeV, dp/p : 0.002- \rightarrow 0.01, dz : 5m- \rightarrow 1m



approaching transition:

- RF rotation voltage dominated by space charge

$$V \sim \eta / \chi^2 + (\eta \Sigma_f) / (1 + \chi)$$

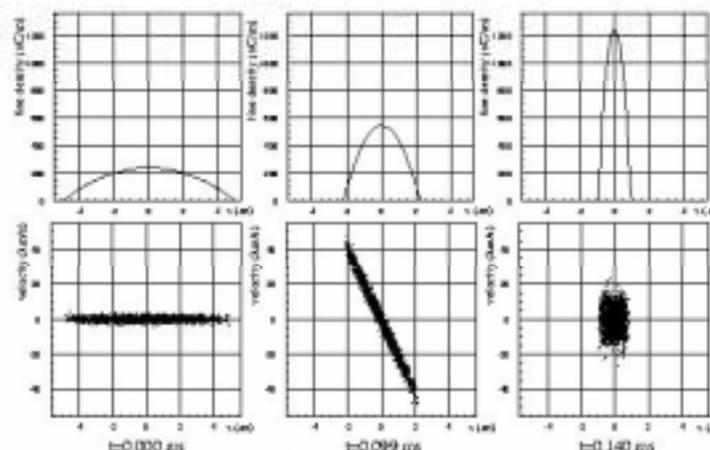
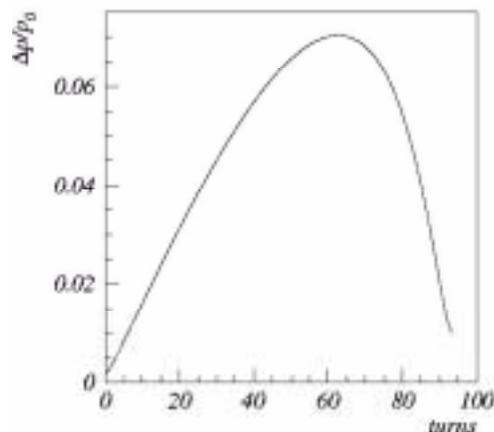
χ : compression factor

η : slip factor

Σ_f : space charge parameter ($\sim U$)

$$= 3g_0 N_b r_p / (\beta^2 \gamma^2 \eta z_b \delta p / p^2)$$

- increasing over-rotation

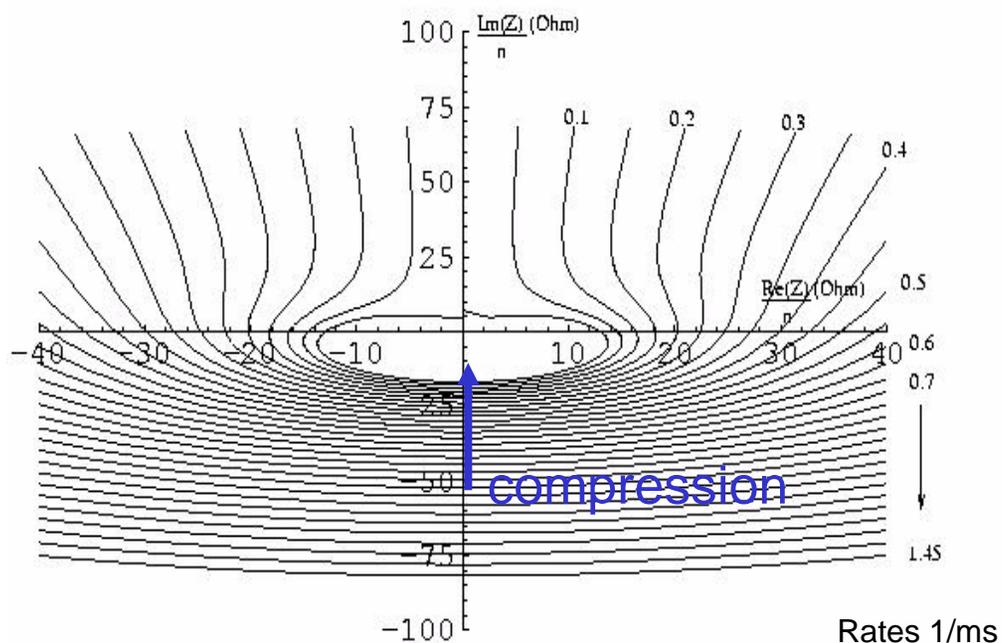


* G. Franchetti, I. Hofmann and G. Rumolo, PR-STAB (2000)

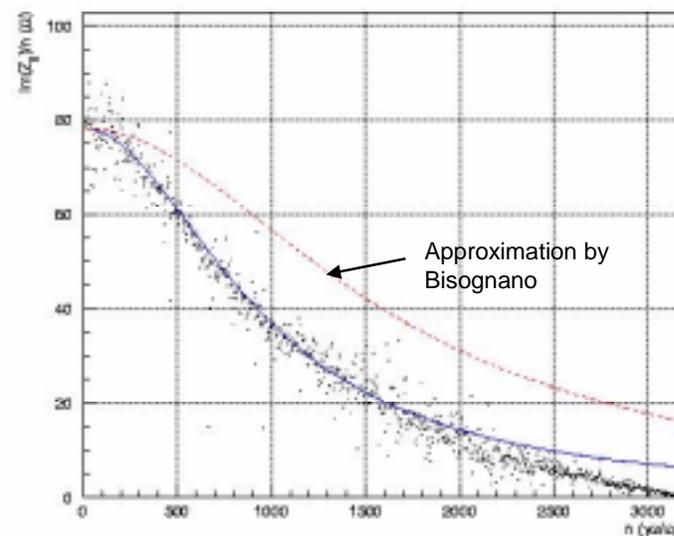
Above transition „attractive“ effect of space charge *

Space charge supports

- envelope rotation
- also growth of higher order modes



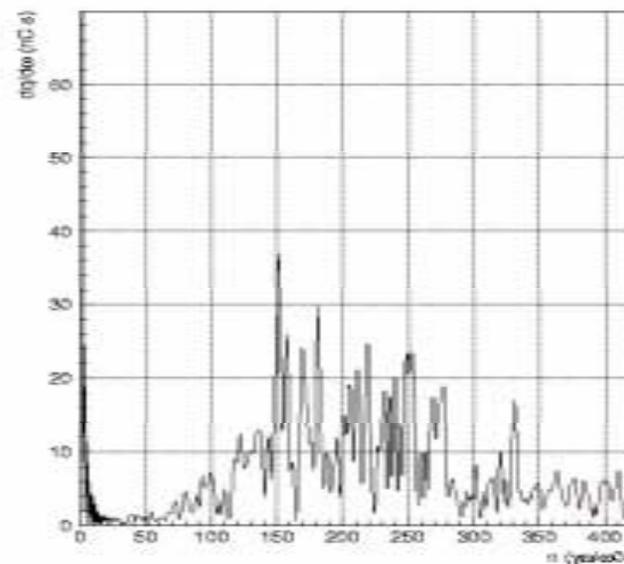
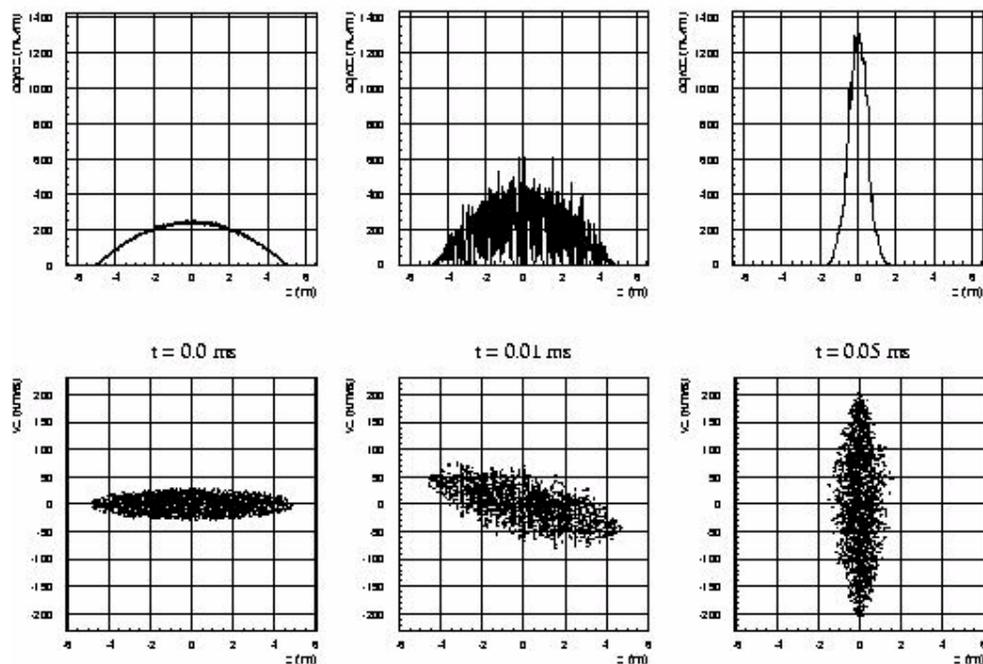
Reduced coupling impedance for very short wavelengths:



* G. Rumolo and I. Hofmann, PAC01

PIC-simulation in r-z (constant focusing)

- Negative mass modes are non-propagating ($\text{Re } \omega \rightarrow \text{Im } \omega$) purely growing
- Rotation must be faster than growth of negative mass modes - „mixing of modes“ helps during rotation

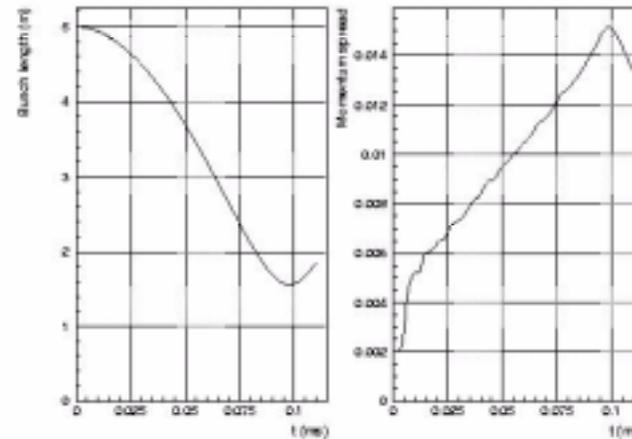
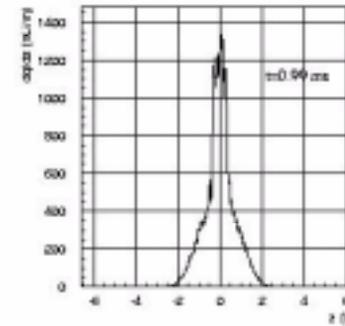
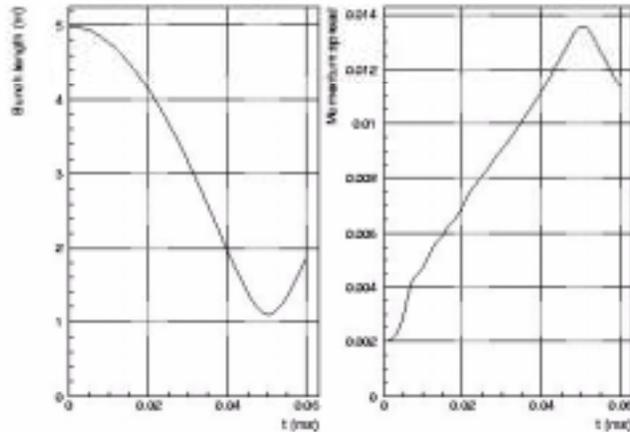


spectrum

Approaching transition from above limited by negative mass instability to a space charge parameter $|\Sigma_i| \sim 5$ (final working point inside K.-S. circle)

broadend shoulders for
 ~ 2 times smaller η

Optimum case: Rf voltage saving ~ 2 above transition

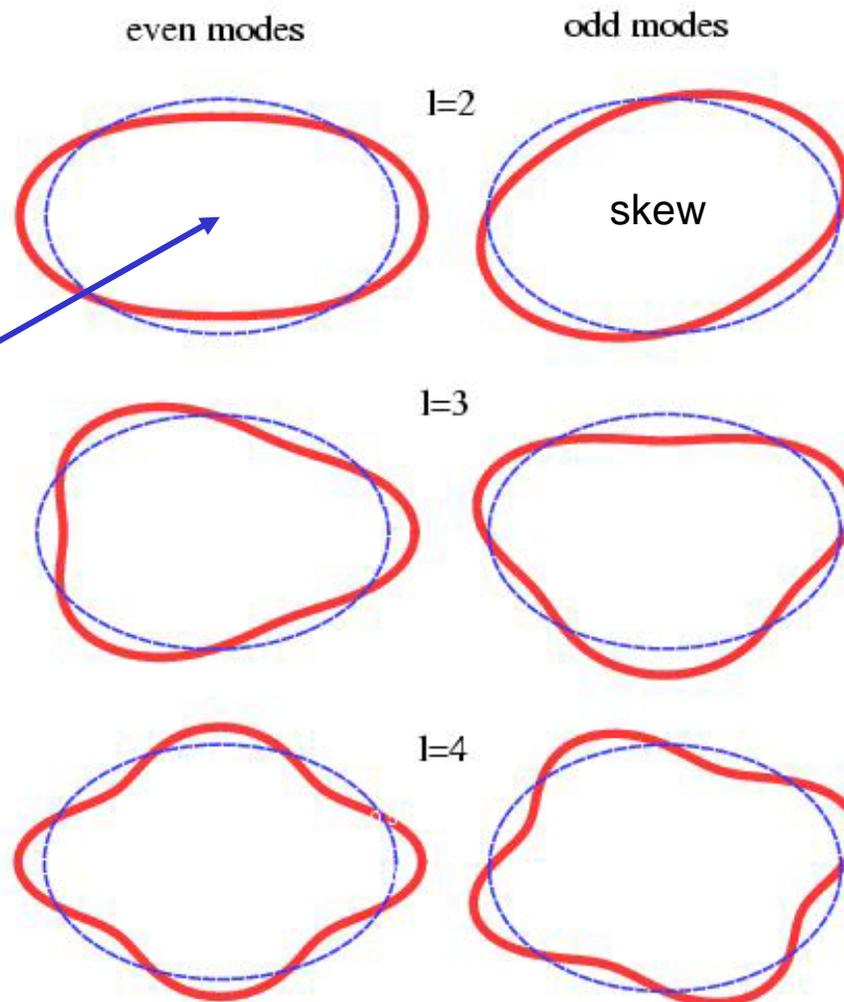


Transverse Space Charge Issues

Modes of transverse density oscillations

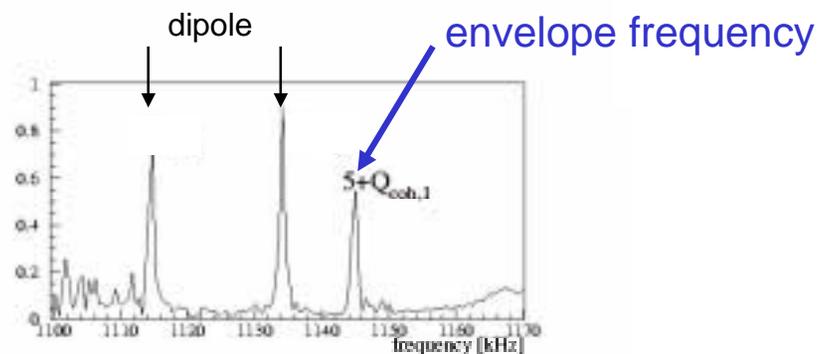
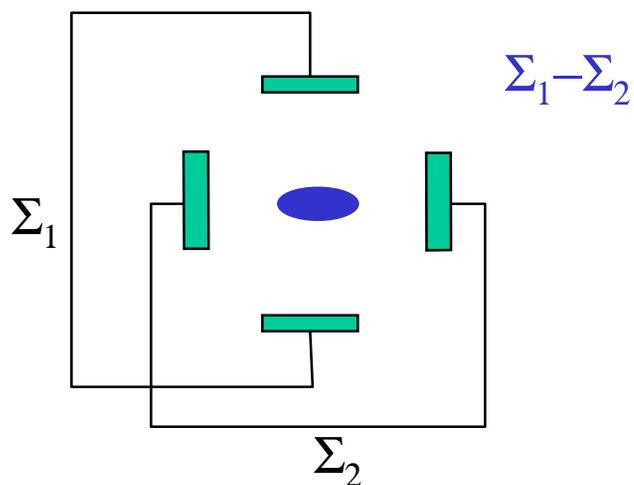
- coherent shift for resonance crossing
- emittance transfer

2 envelope modes (breathing and quadrupolar) can be observed with quadrupolar pickup



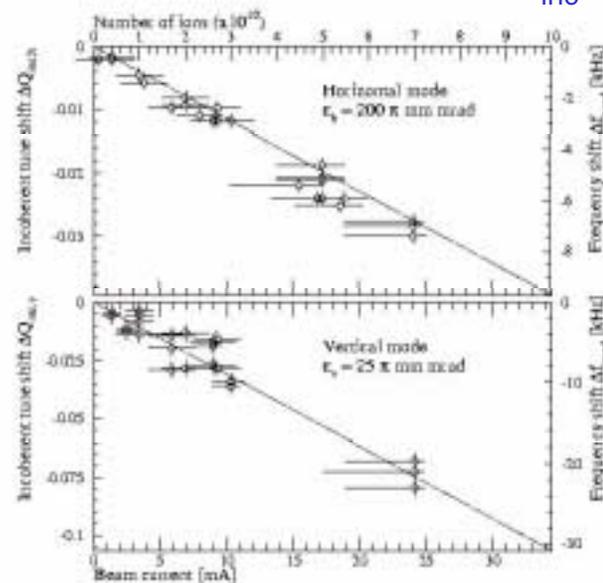
Quadrupolar Pickups to measure coherent envelope frequency shift (coasting beam)

- excited beam with swept frequency
- recorded response



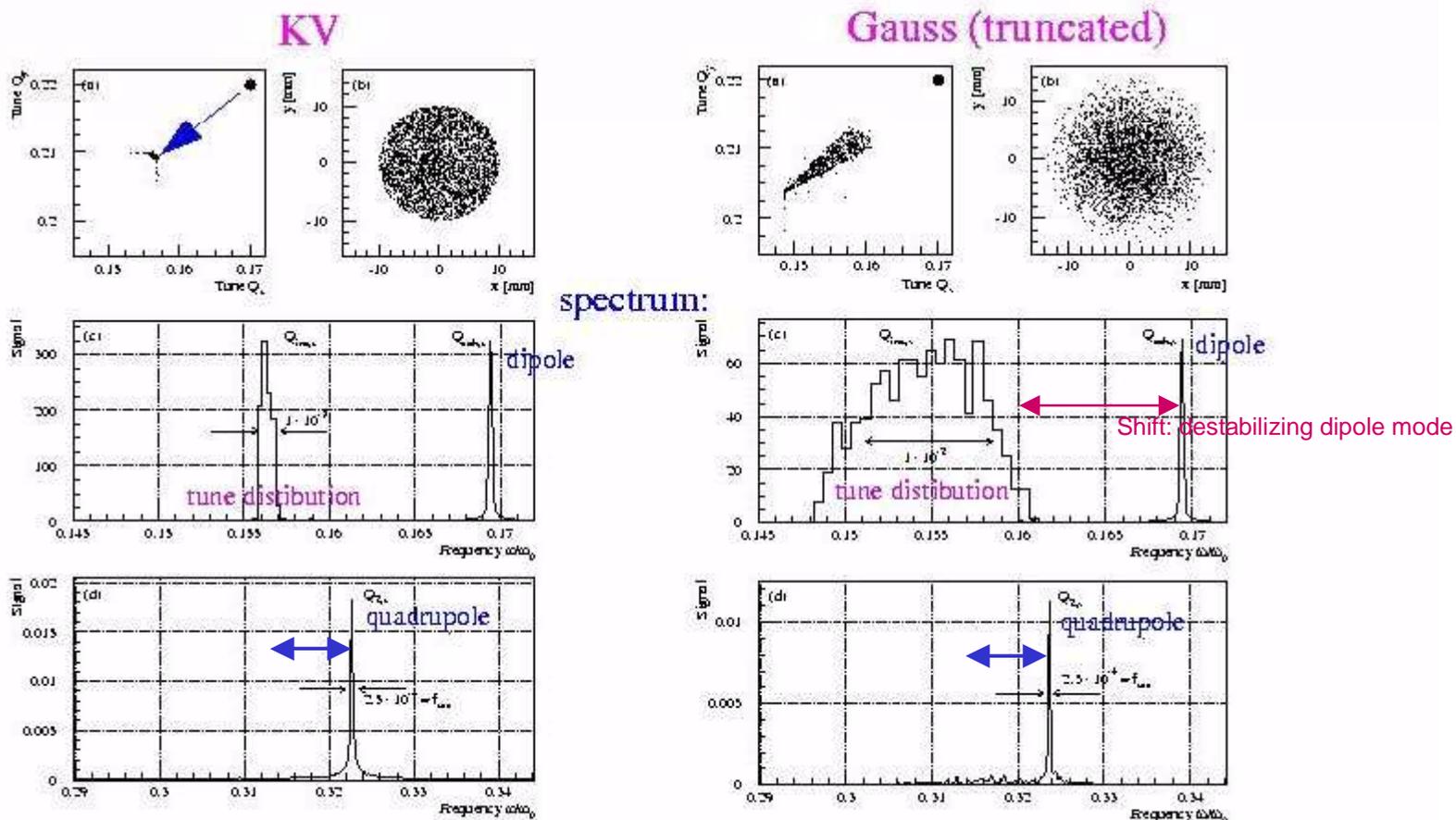
used it to determine ΔQ_{inc} or ϵ_{rms}

$$Q_{coh,1} - 2Q_{o,x} = (3 - a(a+b))\Delta Q_{inc}$$



Coherent frequency shift - no incoherent signal observed

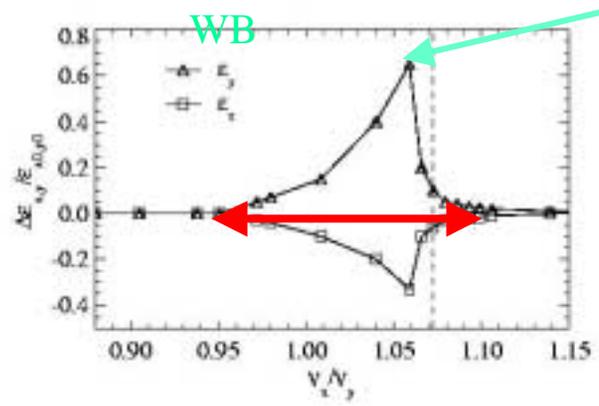
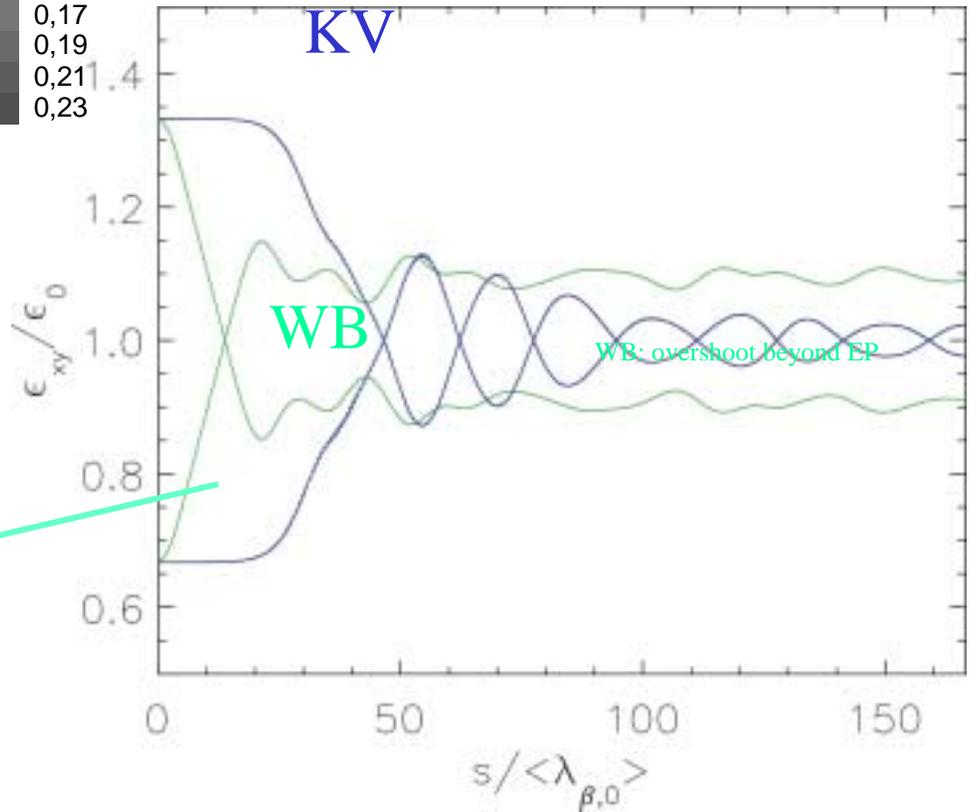
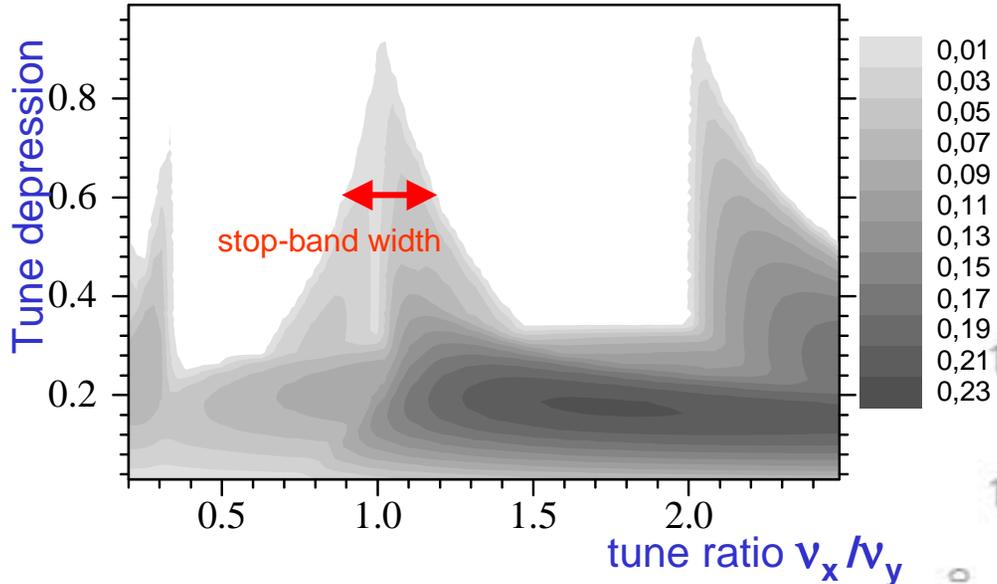
- 2D PIC-simulation to analyze noise very useful
- for injection imprint (SNS ring etc.)
 - bunched beam effect
 - significant sampling times may be needed
 - great challenge to parallel computing



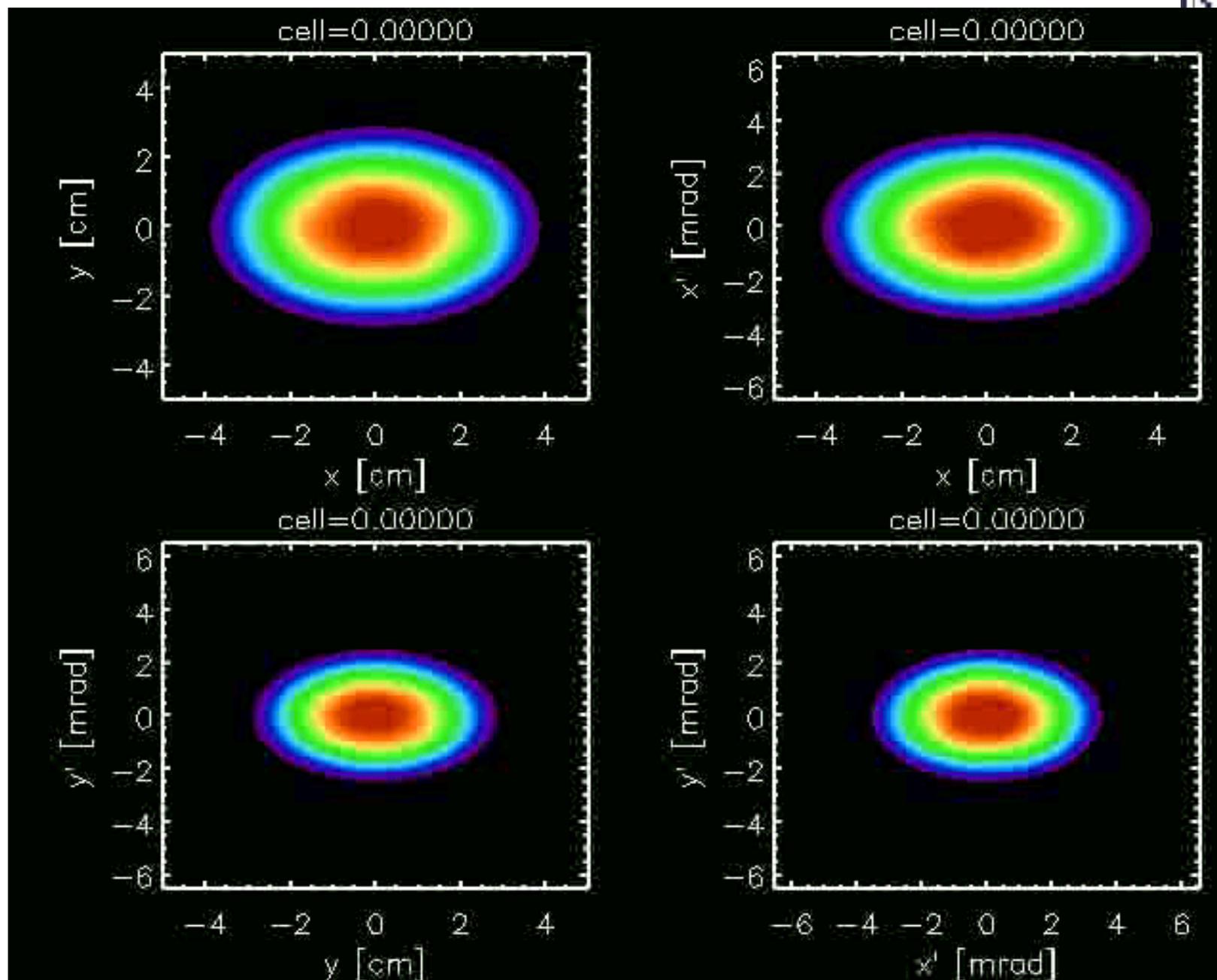
Higher – 4th order – known as “Montague-resonance”: $Q_{x0}/Q_{y0} \sim 1$

- Montague, 1968 CERN-68/83
- need to split tunes to avoid $2Q_y - 2Q_x = 0$ driven by nonlinear space charge force from non-uniform beam $V_{sc} \sim a(x^2 + y^2) + b(x^4 + x^2 y^2 + y^4) + \dots$ leading to emittance transfer from horizontal to vertical in *ideal* lattice
- Montagues analysis was *incoherent* – fixed space charge potential – coherent more adequate
- ~ measurement reported at KEK (Sakai et al., PAC01)

Studied space charge driven 4th order resonance in detail using 2D PIC and $v_y/v_{y0}=0.8, \epsilon_x/\epsilon_y=2$ (IH et al., PRL 87/2001)

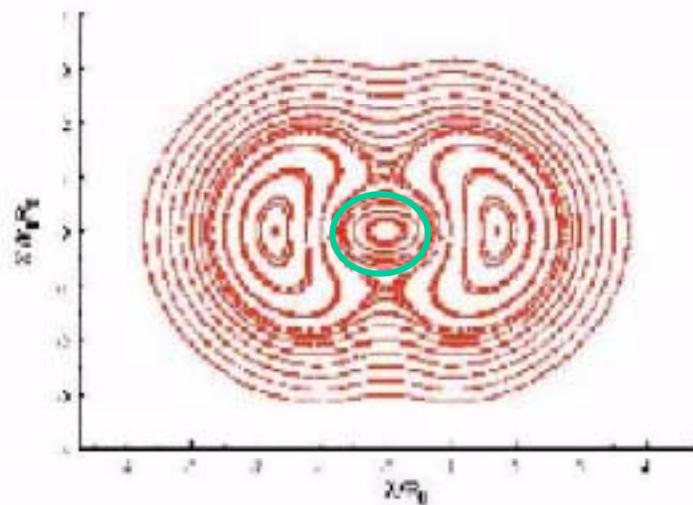


KV: exponential growth takes more time as it grows from noise!



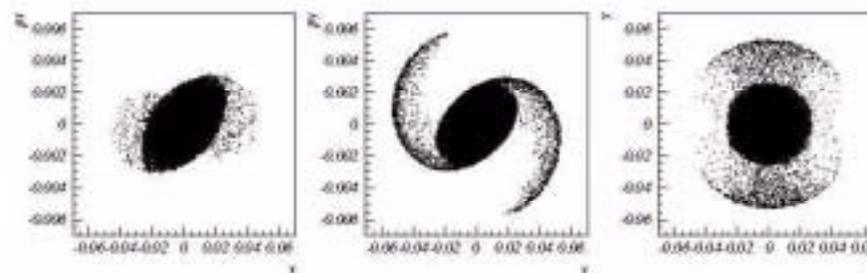
Injection mismatch and halo losses

applied in an idealized model as a first step
to model injection loss into AGS at Brookhaven
- to be extended to bunches and full lattice
(G. Franchetti, I.H., A. Luccio)



↑ ↑
2 fixpoints

Phase Space Plot at $s/\lambda = 40$



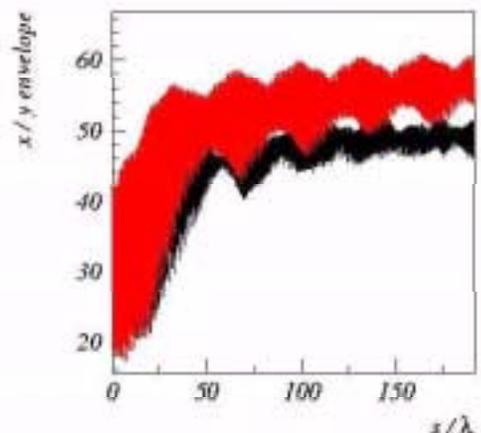
$$v_x / v_y = 0.974$$

Mx = 50%

My = 50%

Results on halo growth depend sensitively on tune split

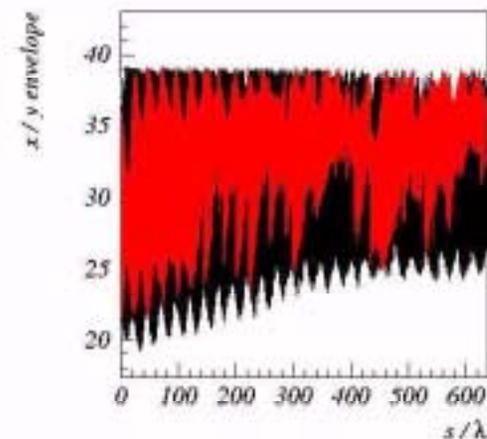
$\delta Q/Q = -0.0294$ $v_y/v_{y0} = 0.95$



en-mismatch-wb-ops-0.95c1.32z1.08-arcl.0z1.5-1.5

maximum size
(mm)

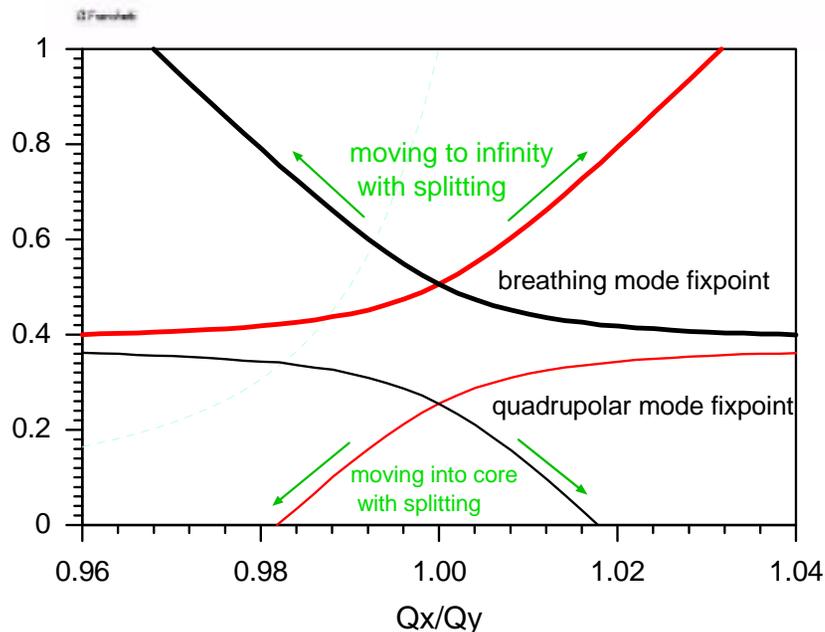
$\delta Q/Q = 0.018$ $v_y/v_{y0} = 0.95$



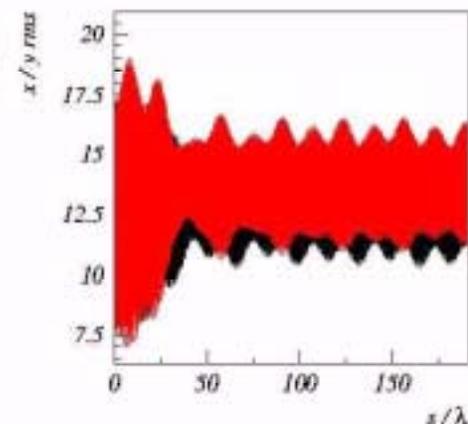
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no damping of rms oscillations
(function of tune split)

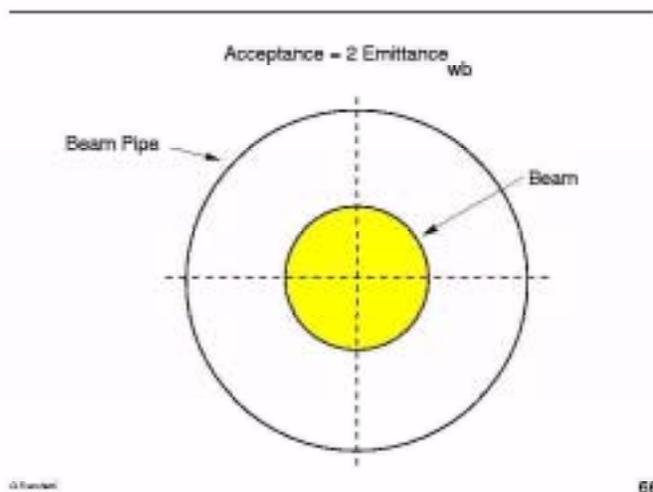


$\delta Q/Q = -0.0294$ $v_y/v_{y0} = 0.95$

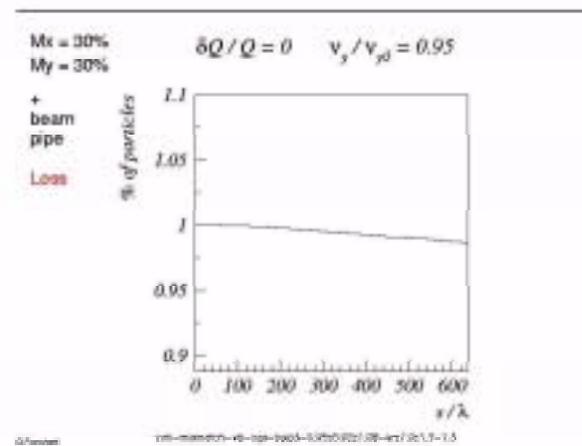


en-mismatch-wb-ops-0.95c1.32z1.08-arcl.0z1.5-1.5

Aperture loss modelling



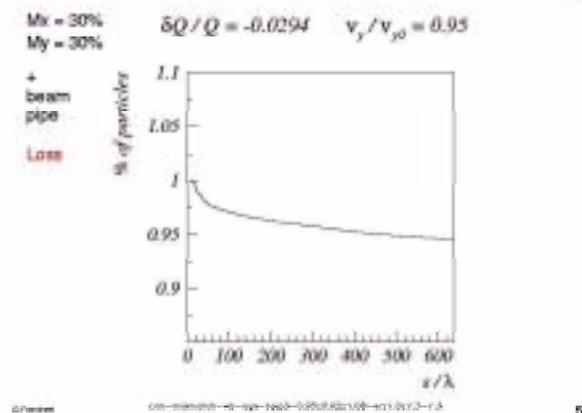
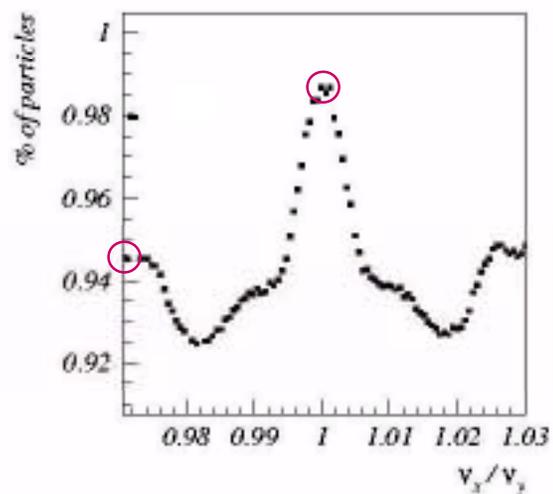
66



68

EFFICIENCY

Mx = 30%
My = 30%



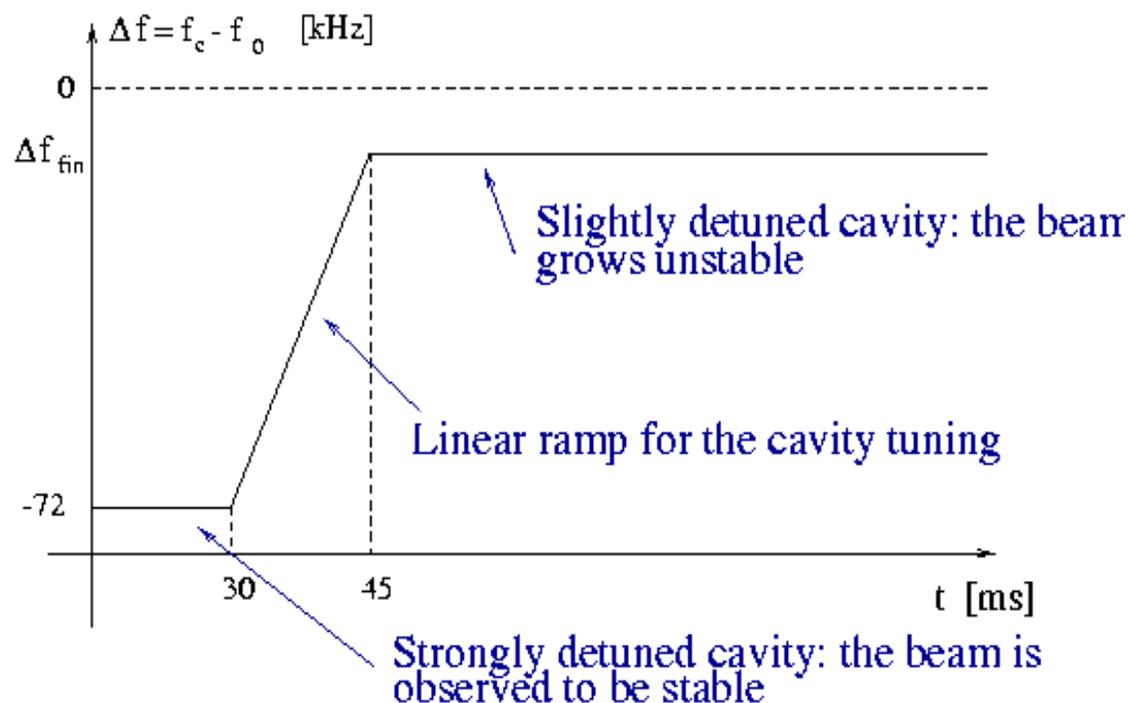
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Concluding remarks

- Coherent longitudinal space charge effect may
 - affect Landau damping
 - stabilize or destabilize (ReZ/ImZ)
 - leave imprint on noise spectrum
- coherent transverse similar
 - dominates quadrupolar spectrum
 - appears in coherent „Montague“
 - mismatch mode damped by halo depending on tune splitting – loss on beam pipe

ESR experiments with e-cooled C^{6+} beam at 340 MeV/u

- prior to the onset of instability the beam adopts a very clean Gaussian momentum distribution due to e-cooling
- RF cavity ($h=1$) destabilizes beam (ecool on or off)
- current signal stored on LeCroy digital analyzer

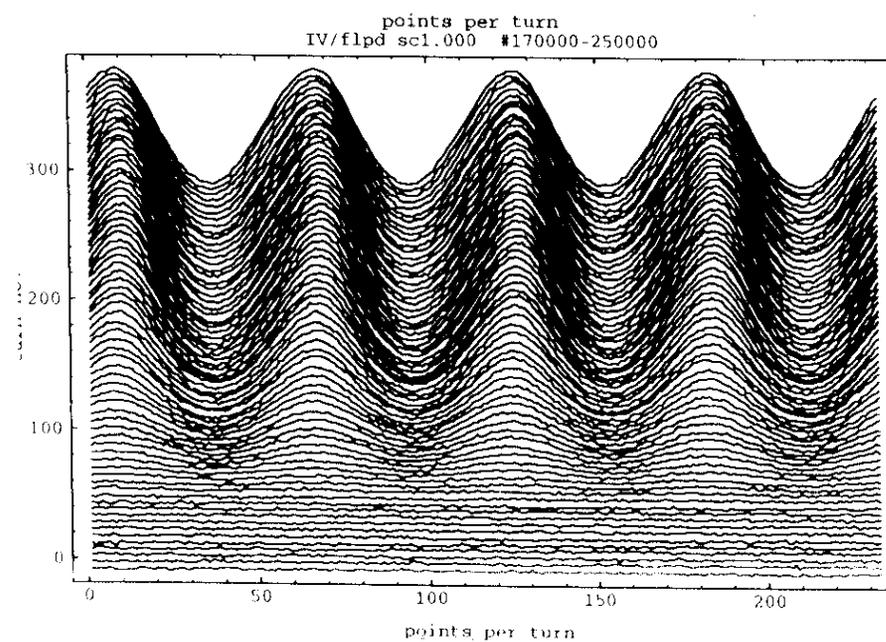
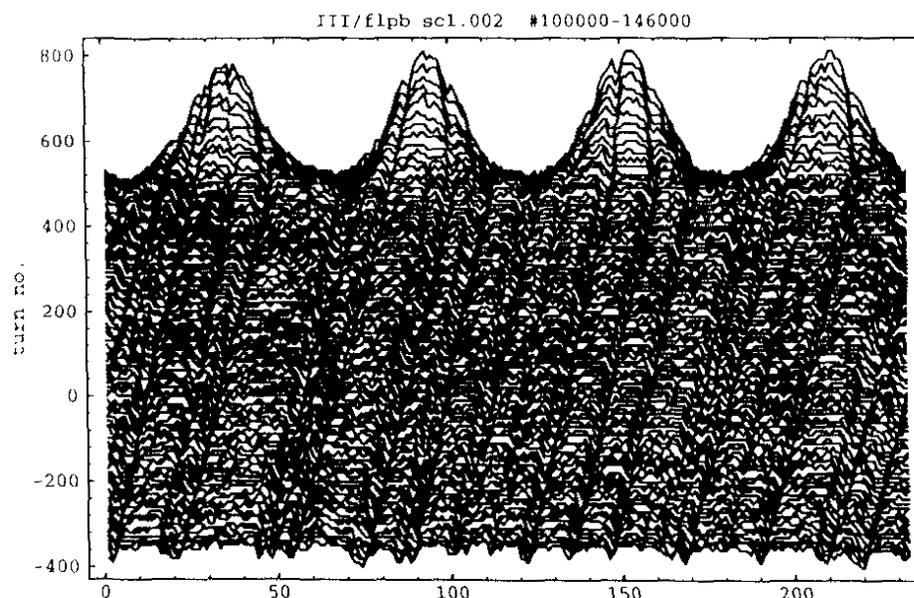


SIS measurement after injection

early after injection of
 $1.5 \cdot 10^{10}$ ions of Ne^{10+} at 11 MeV/u

assume beam was near stability
boundary of Gaussian

allowed 200 ms injection flat-top
 -> smoothing by IBS or Landau
 damping (?)



Holes are continuously trapped in phase space

- wave is generated at lower momentum edge
- the fast instability leads to hole structures traveling in the direction of larger momentum (self-buckets)
- result is a momentum broadening and slight deceleration of beam (energy source=longitudinal motion)

